PVT Compensated OTA Design on SOI-CMOS Nanometer Technologies

By

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“To my parents Mario and Nubia Consuelo, to my sister Andrea and my dear María”

“A mis padres Mario y Nubia Consuelo, mi hermana Andrea y mi querida María”

Francisco.
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SUMMARY

TITLE:
PVT Compensated OTA Design on SOI-CMOS Nanometer Technologies. ¹

AUTHOR:
Francisco Javier Villota Salazar. ²

KEY WORDS: Rail-to-rail input swing, robust design, PVT variations, constant transconductance, high gain, flat-band gain’s variation, nanometer technologies, SOI, OTA.

DESCRIPTION: In this study the design of a PVT compensated rail-to-rail input stage with constant transconductance and a high gain stage are presented, with the aim of providing a robust alternative to the problem of constant transconductance, reduced gain and flat-band gain’s variation of amplifiers in nanometer technologies.

Initially, an overview about the main concerns to downscaling in transistor sizing and some characteristics and details about SOI nanometer technology are given in order to identify the advantages and drawbacks with respect to CMOS technology. Subsequently, a solution to the sizing problem in current technology is adopted, which make the design of circuits possible. A rail-to-rail input stage with constant transconductance is designed, whose outstanding characteristics are the high robustness to PVT variations and the easy integration with other stages. These characteristics are obtained using the Feedback Differential Pair (FDP) circuit, improving the biasing, sub-threshold region for input differential pairs and an addition current circuit with opposite behavior in temperature with respect to the input signal section.

For the gain stage design, first the problem of flat-band gain’s variation had to be solved. Then, some topologies to obtain high gain are reviewed, and at the same time some design considerations are reviewed and proposed in order to identify robust topologies. Applying these considerations and the transconductance addition technique, a two stage amplifier with two transconductance additions is proposed, which reaches a high gain value without using cascode structures or boosting techniques. Finally, the two designed circuits are integrated as an OTA circuit, which is fully characterized including PVT and Monte Carlo simulations in order to verify that all the design considerations were correct.

¹Master project
²National Institute for Astrophysics, Optics and Electronics. Advisor Ph.D Guillermo Espinoza Flores-Verdad.
RESUMEN

TÍTULO:
Diseño de OTA compensado en PVT en tecnologías nanométricas SOI-CMOS. ³

AUTOR:
Francisco Javier Villota Salazar. ⁴

PALABRAS CLAVE: Rango de entrada riel a riel, diseño robusto, variaciones PVT, transconductancia constante, alta ganancia, variación de ganancia en banda plana, tecnologías nanométricas, SOI, OTA.

DESCRIPCIÓN: En este trabajo se presenta el diseño de una etapa de entrada de riel a riel con transconductancia constante y una etapa de alta ganancia, con el objetivo de proporcionar una alternativa robusta a los problemas de obtener transconductancia constante, baja ganancia y variación de esta en bajas frecuencias para los amplificadores en tecnologías nanométricas. Inicialmente se presenta una breve introducción acerca de los principales inconvenientes de la reducción de tamaño en las dimensiones del transistor, luego se explican algunas características y detalles acerca de la tecnología SOI de escala nanométrica, esto con el fin de identificar las ventajas y desventajas con respecto a la tecnología CMOS. Posteriormente, se adopta una solución al problema de dimensionamiento en la tecnología empleada, lo cual permite el diseño de los circuitos en la tecnología anteriormente mencionada. Se diseña una etapa de entrada de riel a riel con transconductancia constante, cuyas características más sobresalientes son la robustez a variaciones PVT y su fácil acoplamiento con otras etapas. Estas características se obtienen usando el circuito de par diferencial realimentado (FDP), mejorando la polarización, la región de sub-umbral para los pares diferenciales de entrada y un circuito de suma de corrientes con comportamiento opuesto en temperatura con respecto a la sección de entrada de señal. Para el diseño de la etapa de ganancia, primero se resuelve el problema de variación de ganancia en baja frecuencia. Entonces se revisan algunas topologías para obtener alta ganancia, al mismo tiempo se proponen y revisan consideraciones de diseño con el fin de identificar las topologías robustas. Aplicando estas consideraciones y la técnica de suma de transconductancias, se propone un amplificador de dos etapas con dos sumas de transconductancia, el cual alcanza valores altos de ganancia sin el uso de estructuras tipo cascado o técnicas de boosting. Finalmente, los dos circuitos diseñados son acoplados como un OTA, el cual es completamente caracterizado incluyendo simulaciones PVT y Montecarlo con el fin de verificar que todas las consideraciones de diseño fueron correctas.

³Proyecto de Maestría
⁴Instituto Nacional de Astrofísica, Óptica y Electronica. Director Dr. Guillermo Espinoza Flores-Verdad.
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Acronyms

CMFB Common Mode Feedback.
CMOS Complementary Metal Oxide Semi-Conductor.
CMRR Common Mode Rejection Ratio.
DIBL Drain-Induced Barrier Lowering.
FD Fully Depleted.
FDP Feedback Differential Pair.
FET’s Field Effect Transistors.
GBW Gain-Bandwidth Product.
IC Integrated Circuit.
OTA Operational Transconductance Amplifier.
PBT Parasitic Bipolar Transistor.
PD Partially Depleted.
PSRR Power Supply Rejection Ratio.
PVT Process Voltage Temperature.
SC Switched Capacitor.
SCE Short Channel Effects.
SOI Silicon on Insulator.
THD Total Harmonic Distortion.
Chapter 1

Analog in Nanometers

This chapter presents a short discussion on how trends in digital circuits force analog designers to develop and propose different solutions to make analog circuits in digital technologies; next is an analysis of how Short Channel Effects (SCE) stop the downscaling in Complementary Metal Oxide Semi-Conductor (CMOS) technology to analog design, and the advantages of Silicon on Insulator (SOI) technology. Then characteristics and restrictions of the technology used to develop this project are discussed, along with some considerations about Process Voltage Temperature (PVT) simulations. Throughout the chapter drawbacks will be presented that make it difficult to obtain some specifications such as gain in nanometer technologies. Finally the chapter will review works related to amplifiers in this type of technology, desired specifications and drawbacks to achieve them.

1.1 Introduction

Downscaling of technology is a continuous process in the semiconductor industry, due to the trends and the requirements of the industry itself, as well as related industries. Scaling transistor size allows the development of smaller circuits and devices, with better performance and lower power consumption, representing increased revenues for all stages of the production chain, and, therefore more satisfied customers. The foregoing represents a general overview, and as will be discussed below, the reduced channel length in current technologies involves many phenomena and complications in the circuit design process.

Reducing the channel length is the main objective in order to improve performance in digital circuits from the technological point of view, since the trend in the electronic industry is to try to avoid the use of analog circuits because most digital circuits have greater
advantages in design, automation, fabrication, cost and performance. These characteristics motivate the reduction of transistor dimensions; however, there are some circuit blocks which, by default, either generate or process analog signals such as: data converters, sensors, very low frequency filters, and some specific-purpose circuits among others.

It is clear that the semiconductor industry also develops according to the needs of digital circuits, but analog circuits are not going away, and for that reason digital circuits are mostly fabricated in modern technologies (nanometer), while analog circuits are used in older technologies (micrometer) in order to avoid the drawbacks of reduced channels. Although the previous resource seems to be a reasonable solution, most systems incorporate circuits that use both types of signals (mixed-signal circuits). Due to this, it is not desirable for a system to have two fabrication processes, circuits and dies to handle signals, since this increases the cost of the system and reduces performance due to the additional connections and interfaces between chips.

So far, amplifiers are the most representative analog circuit, and this basic circuit is incorporated in almost all building blocks to develop more complex systems, for instance: data converters, reference sources and filters, among others. This circuit is the base of the analog design, but its development in deep nanometer technologies (under 65nm) has been limited because transistor characteristics are not suitable to develop useful gain, and are affected by new distortion sources, making the design process more difficult and restricting.

On the other hand, it is known that PVT variations are the main concern for getting robust circuits. The uncertainty is due to the non-idealities in the fabrication process and the wide range of environmental conditions, both outside and inside the chip. PVT variations significantly affect internal parameters of the transistor. In analog circuits all the circuit specifications are developed from these parameters, so it follows that compensating or eliminating variations must be a priority in nanometer technologies because the effects on circuit performance can easily be rendered useless.

The focus, therefore, is the design of amplifiers considering two important criteria: the analog blocks (especially amplifiers) must be designed with functional specifications in nanometer technologies, and the circuit must be robust to PVT variations. In addition, this thesis will analyze three aspects that make amplifiers more useful in complex systems: rail to rail input, high gain and reduce the distortion sources.
Next, the problematic and technological aspects that surround amplifiers design in nanometer technologies will be discussed.

1.2 Short Channel Effects, Scaling and Technology

With the continuous scaling of transistor dimensions expected phenomena began to appear, but their effects on technologies equal to or more than 1 \( \mu m \) were neglected or easily corrected, therefore the SCE did not represent a big concern. For more reduced technologies, such as 0.13 \( \mu m \) or 0.18 \( \mu m \), it was necessary to consider these drawbacks in the design stage, including these effects in the mathematical model. Also, design techniques were implemented to mitigate negative effects.

The previous solutions to work in presence of SCE allow the survival of analog circuits in micrometer technologies; however, the quantity and diversity of analog circuits between 65 nm and 90 nm for Bulk-CMOS\(^1\) technology are dramatically reduced to a few blocks and basic circuits. Under 65 nm is virtually null due to the increase in the SCE incidence. This brief analysis shows the importance of develop new techniques and strategies that allows the analog design in nanometer technologies, because the analog building blocks always be necessary in any scale of technology.

1.2.1 Non-viability of scaling in CMOS to analog design

Since the second half of the last century, the use of CMOS technology has provided the most important basis to the industrial world due to its quick development, scalability, and low cost to produce a large number of devices. However, its weaknesses have been exposed with the emergence of nanometer technologies, such as the non-viability of continued scaling. Apart from limitations in the manufacturing process and materials, the weaknesses are due to the following reasons [1,7]:

- The reduction in transistor dimensions: the charge transport only occurs on the surface of the device, making the bulk terminal useless, and the presence of unwanted effects like latch-up, punch-throught and Drain-Induced Barrier Lowering (DIBL), among others.

- The high value of leakage currents, which in some cases reach the order of bias current.

\(^1\)henceforth be called only CMOS
- Static power consumption is similar to dynamic power consumption.
- Poor immunity to noise coupled through substrate.
- Threshold voltage cannot be reduced in the same order as the transistor size.
- Due to the above, nominal bias voltage cannot be reduced in the same scale as technology.
- With smaller devices and a bias voltage that is not scaled to the same size, horizontal and vertical fields rise, increasing the incidences of other effects over mobility, such as saturation and degradation.
- In general, all SCE become more pronounced and generate more undesirable effects in circuit performance.

Thus, it is clear CMOS technology is not suitable for deep nanometer technologies and it is necessary to incorporate analog circuits in modern technologies in order to obtain all the benefits they can offer, as discussed below.

1.2.2 Silicon on insulator technology

Contrary to what is generally believed, SOI technology development is not unique to the last decade. SOI emerged in the 70s and was only used for specific applications because of the overwhelming success of CMOS. As discussed above, CMOS was successful due to the fast growth and scalability that allow rapid improvements in circuit performance by several orders of magnitude. Even so, a decade ago the limits of that technology became evident, such as the non-viability of maintaining scale, and it was necessary to deal with new technologies or improve the existing ones. SOI-CMOS\(^2\) technology developed a better and more efficient fabrication process, giving rise to a high-quality and low-cost process that mitigated (or eliminated, in some cases) the drawbacks of CMOS. Thus, SOI took the next step in terms of scaling, because unlike other technologies, SOI preserves the same principles of operation and is compatible with current manufacturing processes [1,7].

The SOI manufacturing processes are similar to the CMOS, but some new techniques are applied. The four techniques used to generate a SOI wafer are: Smart Cut, BESOI, ELTRAN and SIMOX. The first one is the most widely used, accounting for more than 80% of production in 2007. For more information about the manufacturing process for

\(^2\)henceforth be called only SOI
each technique, the reader may consult references [1, 7, 8]. Next, some features of this technology will be described.

A SOI circuit consists of separate devices made in silicon islands, which are dielectrically isolated (laterally and vertically) as shown in figures 1.2 and 1.1(b). Horizontal isolation provides a compact and technologically simplified design, while the vertical isolation is the reason for the technology’s name, which is based on the benefits of SOI. These benefits explained below, allow higher speed, very low power consumption, and higher temperature functional circuits. The main advantages of this technology are:

- The current technology offers processes and high quality wafers at competitive costs.
- Due to the vertical isolation, junction capacitances are considerably reduced, thereby increasing circuit speed and reducing power consumption.
- With a small or zero bulk section, some second-order effects are eliminated, such as latch-up, punch-throught and DIBL, among others.
- Technology can be scaled without increasing the incidence of short channel effects. This refers to the incidence of these effects on CMOS technology, which include scaling the threshold voltage.
- Scaling the threshold voltage reduces the supply voltage, which is reflected in the reduction of power consumption.
- It reduces the supply voltage compared with dimensions so the magnitude of the electrical field inside the device can be reduced in order to mitigate some SCE.
- The substrate is isolated, so no noise is coupled through this. But the charge accumulation in floating body generate an important noise contribution CMOS.
• It removes the harmful and widely known effect of latch-up.

• In general, all SCE are reduced and some are eliminated, making it is possible to continue with downscaling in technology.

Apparently SOI technologies emerge as an indisputable alternative, but also bring new problems and limitations that must be taken into account by the designer. The main difficulties are shown below, and most of them only affect the partially depleted transistors. The main differences between the two kinds of transistors of this technology will be explained later.

• Kink effect: impact ionization of the majority carriers causes the accumulation of charge in the floating body, reducing the threshold voltage and producing a sudden jump in drain current as shown figure 1.2. It causes a variation in body potential and noise.

• Hysteresis: charge accumulated in the body modifies the transistor behavior when it changes the operating region, producing a different behavior when the transistor makes the transition from cutoff to strong inversion and vice versa. In extreme situations this charge accumulation can provide a channel independent of biasing, giving rise to a latch and making the device useless.

• History effect: Transient behavior of drain current is not constant over time, since it depends on the previously accumulated charge in the body and operation point. It can generate over- or under-shoots when the settling time is defined by recombination and generation processes. The designer must take into account not only spatial variations, but also temporal variations and uncertainty in current behavior.

• Parasitic Bipolar Transistor (PBT): A parasite transistor is created inside the device with a drain terminal-like collector, source-like emitter and floating body as a base. The PBT induces a premature rupture (in both SOI transistors), generating another jump in drain current as shown figure 1.2, but this jump occurs at a higher potential with respect to the kink effect.

• Second channel: Between the insulating layer and the substrate exists another interface of materials. This interface generates a second channel in which current flow must be taken into account in some cases, especially for fully depleted transistors.

• Self-heating: The insulating layer has a high thermal resistance and prevents the release of energy, raising the internal temperature and modifying the transconductance of the device, among other internal parameters.
1.2 Short Channel Effects, Scaling and Technology

Figure 1.2: Incidence of kink and PBT effects on drain current-voltage characteristic.

Most of the phenomena previously referred has been modeled and simulated in professional tools like Hspice or Cadence [7]. Subsequent sections provide details about some specific characteristics of these phenomena that must be taking into account for the simulations in the present work.

Some characteristics about SOI were presented. However, this analysis does not indicate that analog circuit design in nanometer technologies would be easier since the presence of SCE remain strong (but in CMOS it is absolutely impossible). In subsequent chapters, it will be analyzed why practically does not exist analog design in this technology despite the technological benefits of SOI.

1.2.2.1 Partially depleted vs. Fully depleted

SOI technology offers two types of transistors: Fully Depleted (FD) and Partially Depleted (PD). These transistors are shown in figures 1.3(a) and 1.3(b). The main difference is the thickness of the silicon layer employed to make wells. For PD transistors the thickness is enough to generate an inversion region and a channel, while a little portion of the material close to insulator acts as a body. This bulk has the special characteristic that it is floating and anything controls its potential. The principal advantages of SOI are based on the assumption that the body does not exist inside the transistor. However, a PD transistor has a zone that acts like a body. Although the technological benefits are not affected, it presence generates the problems mentioned previously.

A solution to the body remaining charge was found in FD transistors. The difference is that the thickness of the silicon layer is extremely thin, and the entire region under the
channel is depleted, therefore any charge can be accumulated. This innovation eliminates negative effects like kink and history, among others. It could be thought that the FD transistor is the optimal solution, but this new process is expensive, complex and hardly scalable due to minimal dimensions managed. Also, it is a drastic change with respect to CMOS rather than PD processes. For these reasons PD transistors are more widely employed and will be used in the present work because it is expected that any proposed developments may be functional in the majority of technologies.

1.3 IBM 45 nm Partially Depleted SOI Technology

For the development of this project SOI technology provided by IBM through their 45 nanometer process will be used. The aforementioned technology only incorporates partially depleted transistors whose selection was discussed before. On the other hand, the 45nm process has been used for analog design in [3, 9], being the only references found about the topic under 65nm, moreover considering that the contribution of this work will be easily applicable to similar scale technologies. The information in this section was taken from technology documentation [2].

1.3.1 Overview

Micrometer technologies generally offer two or three kinds of Field Effect Transistors (FET’s) in analog design. In most of the cases, the general purpose transistor is employed because it is widely characterized. On the contrary, the technology used in this project has more than 15 transistor types with different behavior. This fact in fact constitutes another design variable which must be taken into account. The majority of transistors are made to be used in digital standard cells, and some of them can only be used in specific
1.3 IBM 45 nm Partially Depleted SOI Technology

<table>
<thead>
<tr>
<th>Device Type</th>
<th>L [nm] (Restricted)</th>
<th>W [µm] (N/P) (Nominal)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regular $V_{th}$ floating</td>
<td>40</td>
<td>0.4 / 0.6</td>
</tr>
<tr>
<td>High $V_{th}$ floating</td>
<td>40</td>
<td>0.4 / 0.6</td>
</tr>
<tr>
<td>Super $V_{th}$ floating</td>
<td>40</td>
<td>0.4 / 0.6</td>
</tr>
<tr>
<td>Ultra $V_{th}$ floating</td>
<td>40</td>
<td>0.4 / 0.6</td>
</tr>
<tr>
<td>Extra $V_{th}$ floating</td>
<td>40</td>
<td>0.4 / 0.6</td>
</tr>
<tr>
<td>Analog $V_{th}$ floating</td>
<td>56</td>
<td>1.3</td>
</tr>
<tr>
<td>Analog $V_{th}$ body-contact</td>
<td>56</td>
<td>1.3</td>
</tr>
<tr>
<td>Analog $V_{th}$ body-contact A</td>
<td>112</td>
<td>1.3</td>
</tr>
<tr>
<td>Analog $V_{th}$ body-contact M</td>
<td>232</td>
<td>1.3</td>
</tr>
<tr>
<td>Thick oxide floating</td>
<td>112</td>
<td>1.3</td>
</tr>
<tr>
<td>Thick oxide body-contact</td>
<td>112</td>
<td>1.3</td>
</tr>
<tr>
<td>Thick oxide body-contact HVD</td>
<td>160</td>
<td>1.3</td>
</tr>
<tr>
<td>Thick oxide body-contact M</td>
<td>232</td>
<td>1.3</td>
</tr>
<tr>
<td>Thick oxide body-contact L</td>
<td>472</td>
<td>1.3</td>
</tr>
<tr>
<td>Thick oxide body-contact XL</td>
<td>2000</td>
<td>1.3</td>
</tr>
</tbody>
</table>

Table 1.1: IBM-SOI 45nm Devices and channel restrictions

circuits like RAM cells. In table 1.1 some of the transistors present in this technology are presented. Later, a short description will be given about their main differences in order to select the best option for the amplifier design.

### 1.3.2 Transistor selection

A typical SOI technology is mainly a digital technology since most of its transistors offer benefits in digital circuits. Among the transistors found in a SOI technology there are the so-called thick metal transistors, which have nearly two times the thickness of regular transistors. These transistors have a threshold voltage between 400mV and 500mV (also High, Super, Ultra and Extra $V_{th}$), which represents half of the nominal supply voltage, and for this reason these transistors are not suitable for analog design. Additionally, simulations show that some transistors have negative resistance in their characteristic curve and others have multiple slopes in the saturation region.

Other transistors are called body-contact, and are the most similar to CMOS technology because they include another terminal through a parasite transistor (a detailed explanation can be found in [1, 7]) to control the body potential. Since one of the motivations is to obtain all the benefits of SOI, and some of them may be reduced by body contacts, the use of these transistors will only be considered for specific purposes.
According to the previous analysis, two transistors are selected: *Analog* $V_{th}$ and *Regular* $V_{th}$. The first one is the appropriate device for analog design (as its name indicates), whereas the second presents a lower $V_{th}$ than the others, besides having characteristic curves very similar to conventional transistors, unlike the others transistors, which behave abnormally.

### 1.3.3 Behavior of selected transistors

In order to obtain an approximation of transistors parameters, some simulations are conducted, like characteristics and $gm/id$ curves. In the next section some equations are used to establish restrictions and scope of the technology. Figures 1.4 and 1.5 show characteristic curves for two kinds of transistors with the size shown in table 1.1. These figures demonstrate that the channel modulation effect is too drastic because transistors have minimal channel length and the curves exhibit a sudden current increase as a consequence of some of the effects described previously.

In previous curves the behavior presented did not seem dramatic when compared with normal technologies. But if one curve is selected the problem is evident: the saturation region, in which a constant current is assumed, does not exist. Moreover, the modulation channel effect is overwhelming, as figure 1.6 shows.
Transistor behavior is extremely complex and cannot be modeled by relatively simple mathematical expressions allowing a manual design. Because of this, it is necessary to take some measurements in order to establish which specifications can be obtained employing this technology. For these reasons $gm/id$ curves are plotted, since these curves represent a real behavior of transistors, including second-order effects and abnormal behaviors. Four
main features of these curves are explained in [10]:

- Strong relationship between analog circuit behavior and mathematical formulation.
- Provides an indication of operating region.
- Can be used like a tool to size transistor.
- Widely employed at nanometer scale.

Figures 1.7 and 1.8 present $gm/id$ vs. $id/(W/L)$ and $gm/id$ vs. $V_{ov}$ curves for previously selected transistors. For an ideal case, these curves must be independent of transistor
width and drain-source voltage. Given that the range of transistor width is very narrow, was only simulated under nominal conditions. However, each transistor underwent simulations under three different voltages, resulting in consistent curves.

The curves confirm that the transistor should operate in sub-threshold mode in order to implement a gain stage. Moreover, its capacity to develop gain decreases as $V_{ov}$ increases. In the next section, some calculations allow to see the ideal maximum gain of a basic configuration.

### 1.4 Restrictions and Drawbacks in Amplifier Design

In analog design a rule of thumb is to not make any design with minimal channel length (due to SCE effects), and for micrometer technologies it is common use two or three times this length. The major difficulty in this technology is that only one channel length is permitted and modeled, it is the minimum value (40 nm). This is the most important restriction in the technology considered because an analog circuit is never designed with minimal sizes. Moreover, not only is length restricted, but also transistor width because the model is centered in 400 nm for N type and 600 nm for P type ($W_{nom}$), and sets a valid range of simulation between 152 nm to 2.5 $\mu$m [2].

The low supply voltage used in this technology (1 V) does not permit the use of cascode topologies because it reduces the dynamic range at input and output. This makes it difficult to place the transistor in a desired operating point.

With these transistors dimensions it is practically impossible for use in any analog circuit, and some techniques must be implemented in order to obtain a functional amplifier. On the other hand, for some applications it will be necessary to incorporate rail-to-rail amplifier configurations to overcome the low dynamic range available.

Figures 1.7 and 1.8 are useful to determine how much gain can be achieved by a conventional amplifier (a differential pair with active load) and to estimate the maximum gain that the transistor can develop. To determine this value, the highest value from curve is taken and substituted in equation 1.1, assuming it is possible for the transistors to reach this operation point.

$$A = g_{mparr}(r_{on} // r_{op})$$

(1.1)
The results show another widely known drawback about nanometer technologies: the transistors have poor intrinsic gain, which makes it impossible to obtain high gain in amplifiers. In this case the maximum theoretical gain corresponds to 23 dB, and in some simulations it was very difficult to obtain 20 dB. In order to get an idea of the problems posed by the use of nanometer technologies for signal amplification, it must be noticed that it is not difficult to obtain 40 dB in a 0.35 µm CMOS technology.

1.5 PVT Specifications and Simulation

It was mentioned in Section 1.1 that a robust circuit must be functional in spite of PVT variations. In this section it will be explained what these variations mean, their origin, scope, consequences and give a simulation to show their dangerous effects over circuit performance.

- Process variations: The fabrication process is not ideal; some uncertainty exists over transistor parameters and its properties, which generates a very different behavior than expected in simulations. For this reason, the foundry develops special models called corner models, which cover the worst fabrication cases for N or P type transistors, as shown in figure 1.9.
1.5 PVT Specifications and Simulation

<table>
<thead>
<tr>
<th></th>
<th>Minimum</th>
<th>Nominal</th>
<th>Maximum</th>
</tr>
</thead>
<tbody>
<tr>
<td>Process</td>
<td>SS</td>
<td>SF</td>
<td>Typical</td>
</tr>
<tr>
<td>Voltage [V]</td>
<td>0.9</td>
<td>1</td>
<td>1.1</td>
</tr>
<tr>
<td>Temperature [°C]</td>
<td>-20</td>
<td>60</td>
<td>100</td>
</tr>
</tbody>
</table>

Table 1.2: PVT Simulation ranges

For each transistor three models are made: fast, nominal, and slow. They generate a main combination of four corners. As can be observed, the covered area is oval, since it is very probable corners FF or SS occur and less possible cross corners SF or FS occur.

- Voltage variations: Another important issue inside the circuit is the supply voltage distribution, because voltage value varies along circuit connections, and in many points on the chip the real bias voltage is different than nominal supply voltage. It is beyond the scope of this work to discuss the causes which lead to this phenomenon. Generally, integrated circuits are battery-powered. It must be noticed that battery behavior is not linear and constant over time since the voltage it delivers varies with environmental conditions. For these reasons the design generally undergoes to a variation of ±10% over nominal bias voltage.

- Temperature variation: Different places have a wide range of temperatures, and the customer needs the devices to operate satisfactorily under any conditions (temperature). This means that an Integrated Circuit (IC) must operate with the same specifications and at any temperature. But this is a difficult task, because all circuit elements, even connections, modify their properties depending on temperature, and produce heat generated by themselves. A large number of academic simulations are performed at ambient temperature, creating a false environment because this only happens when the circuit is off (generally, the temperature range is between 50 and 80 °C). For that reason, an appropriate simulation range is between -20 to 120 °C.

Table 1.2 shows 11 different characteristics, whose combination generates 45 corners to constitute the PVT simulation for all circuits reported in this document, ranging from a typical case to the most extreme cases, guaranteeing that the circuit will be robust.

Figure 1.10 shows an amplifier’s frequency response simulation in SOI 45 nm technology. The wide black line represents the typical case (which never happens) whose gain is 30 dB. This gain corresponds to the expected value which would be obtained for
the typical case. However, if a PVT simulation is performed the response is far off the expected specifications, leading to an and inappropriate circuit performance. For that reason, making a robust design is the focus of this project.

### 1.5.1 Additional effects covered by simulation

The foundry provides complete models that cover a lot of secondary effects. These models are BSIM-SOI, and are made in Verilog due to the high level required to manage hundreds of equations and terms, in order to simulate effects like self-heating, stress, gate-body tunneling, gate-drain/source tunneling, corner effects (due to their physical location and transistor size), chip orientation, parasite components, and well lengths, among others [2]. In future simulations only functional effects will be considered, and will not consider location effects like orientation or surroundings that correspond to layout extraction.

### 1.6 Rail-to-Rail OTA Design Perspective

In order to get a fair perspective of the design problem of the aforementioned circuit blocks, a search in the state of the art for amplifier design in technologies under 90nm scale is conducted. The results are shown in table 1.3 (at the end of this chapter).
The table shows interesting information: the end of cascode structures, such as folded cascode, is presented in 90nm technology, because the supply voltage is lower, with respect to threshold voltage, and dynamic range is dramatically reduced. The most common structures in nanometer technologies are simple and basic topologies like differential pair and fully differential architectures are suitable to expand output range, and to obtain all the benefits that include this operation mode. The cost is the increase in circuit complexity, and incorporating a Common Mode Feedback (CMFB) circuit in order to tie up common mode output voltage.

It is interesting that any amplifier exceeds 70 dB of gain, including structures like folded cascode with second stage in 90nm. For technologies with more reduced channel length, it is possible to reach 56 dB with special polarization employing the bulk terminal [13]. This work pretends to obtain a reasonable value of gain similar to previous works. Also, this work seeks to obtain a good frequency response for a load near to 300 fF in order to compare with the majority of the related works.

In this chapter was mentioned that in this technology new distortion sources affect circuit performance, and this specification will be taken in account throughout the design process. The rest of this work is organised as follows: chapter 2 presents some design considerations to improve transistor behavior and the design of rail-to-rail input stage. The design process and considerations to obtain high gain in two stages will be presented in chapter 3. Chapter 4 is dedicated to show the simulation results of complete amplifier including rail-to-rail input and gain stage. Finally, some conclusions and recommendations will be presented in chapter 5. In all design stages PVT variations will be taken into account.
### Table 1.3: State of the art.

<table>
<thead>
<tr>
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</tr>
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<tbody>
<tr>
<td>18</td>
<td>1.2</td>
<td>0.96</td>
<td>–</td>
<td>–</td>
<td>0.5</td>
<td>0.2</td>
<td>1.35</td>
<td>–</td>
<td>0.5</td>
<td>–</td>
</tr>
<tr>
<td>180</td>
<td>1.6</td>
<td>0.6</td>
<td>697.33</td>
<td>260</td>
<td>1.35</td>
<td>0.3</td>
<td>20</td>
<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>3</td>
<td>47</td>
<td>0.2</td>
<td>2.5</td>
<td>60</td>
<td>57.3</td>
<td>1.5</td>
<td>2</td>
<td>2.5</td>
<td>57.3</td>
<td>57.3</td>
</tr>
<tr>
<td>0.47</td>
<td>69.6</td>
<td>0.3</td>
<td>1</td>
<td>2.5</td>
<td>37</td>
<td>70</td>
<td>2</td>
<td>70</td>
<td>37</td>
<td>37</td>
</tr>
<tr>
<td>1</td>
<td>0.96</td>
<td>0.6</td>
<td>697.33</td>
<td>260</td>
<td>1.35</td>
<td>0.3</td>
<td>20</td>
<td>0.5</td>
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</tr>
<tr>
<td>1.2</td>
<td>0.3</td>
<td>2.5</td>
<td>60</td>
<td>60</td>
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<tr>
<td>1.3</td>
<td>1.2</td>
<td>0.96</td>
<td>–</td>
<td>–</td>
<td>0.5</td>
<td>0.2</td>
<td>1.35</td>
<td>–</td>
<td>0.5</td>
<td>–</td>
</tr>
</tbody>
</table>

|---------------|------|------|------|------|------|-----|-----|
Chapter 1 shows the drawbacks for sizing in nanometer technologies and the poor transistor behavior. I will be now shown in the first part of this chapter how to improve transistor behavior and how to emulate different sizes over it in order to obtain a device suitable for analog design. In the second part, an analysis about structures with rail-to-rail input characteristic with a constant transconductance ($g_m$) value will be made. Based on this analysis, a new circuit with a $g_m$-constant characteristic is derived. The new circuit is robust to PVT variations over the common mode input range.

2.1 Improving Transistor Behavior

Due to technology features such as low supply voltage and poor intrinsic gain, it is interesting to analyze some techniques that are used in low-voltage circuits such as:

- Sub-threshold operation
- Self-cascode

From previous techniques, the first one will be employed in this chapter to obtain a linear transconductance behavior, and in the next chapter this technique will be used to achieve the highest gain possible. In addition, the second one (also called compound transistor) provides a simple way of increasing the channel length of a single device saving the DC characteristics [15], the last one has been employed to analog design in nanometer technologies [3,9,13]. For these reasons, compound transistors will be explained in detail below.
2.1.1 Compound transistor

Figure 2.1 represent a general scheme of compound transistors. Reference [15] shows that the DC characteristic of this arrangement of transistors is equal to a single device while the following equation is satisfied. Through a mathematical description it can be demonstrated that the cut-off frequency of the compound transistor is higher regarding a single device. On the other hand, the output impedance is increased, but the transconductance is lower than in a single equivalent device.

\[
\left( \frac{W}{L_a} \right) = \left( \frac{W}{L_1 + L_2 + \ldots + L_n} \right) \tag{2.1}
\]

These type of devices have other benefits, such as increased robustness with respect to mismatch and random variations of offset [16], and less sensitivity to \(V_{th}\) variations because the addition of fragmented channel variations are lower [17]. Between all the benefits, the most useful is its capacity to create an equivalent device without minimal channel length, more robust, and with lesser incidence of SCE. The latter improvement makes it possible to increase the gain of amplifiers.

Unfortunately, all the features of this structure are not positive since the transconductance is lower as the number of serial transistors is increased. In the same way, a major value of drain-source voltage is necessary, reducing available dynamic range in the amplifier [18]. Another interesting feature is that for conventional transistors, the lower transistor remains in the saturation region, while the others in triode. In this technology,
the intrinsic parameters have different relationships, even if all of the transistors are the same, they could be in saturation or not at the same time, and still working like an unique transistor. This means that the characteristic that only one remains in saturation is not longer accurate.

### 2.1.2 Transistors Matrix

Compounds transistors can be seen like a serial connection in which the channel length is divided. In the case of width, parallel connection is more commonly employed due to its analogy with fingers in the layout, it represents the solution to the narrow range of values that the technology supports. The principal benefit is that the equivalent device is less sensible to mismatch [15] and provides a wide range of possible widths to simulate.

At the moment have been adopted two techniques to solve the sizing problem in transistors. Now, some simulations are performed to establish if the solution really obtains a better performance in behavior, mismatch, and PVT variations. Figure 2.2 shows a simulation of a single transistor with a ratio \((W/L) = 0.6\mu m/40nm\), and a second curve with the same relationship but in a matrix of 3x3 single transistors. This specific arrangement was made in order to obtain a similar current magnitude while preserving at the same time the simulation range as well as restrictions about sizing in models. The result is very clear, the main advantage show in continuous line is an important reduction of
SCE, specially channel modulation effect. Now, the transistor curve is more similar to a conventional curve suitable to analog design.

Figure 2.3 shows the comparison of a Monte Carlo analysis. Here, continuous lines represent the transistor matrix and the dotted lines represent the single transistor. Only 6 samples corresponding to extreme cases over 100 simulations was plotted for each tran-
sistor type. A slight reduction in dispersion close to 8% of total variation between curves is observed. Figure 2.4 shows the result of PVT simulations, and presents the improved behavior explained before. An advantage respect to PVT variations is that single transistors present multiple slopes and crossing between curves, it generates distortion and makes it more difficult to compensate the circuit. Nevertheless, matrix transistor presents a deterministic behavior and only one slope over saturation region.

2.1.3 Limits and justification

Just like previous analysis, other simulations with a different number of serial transistors were made and it was determined that a reasonable number of transistors per column is 3. With 2 transistors per column the improvement in behavior is not enough since single transistor behavior is very poor, and 4 transistors represent a strong limitation to obtain the desired rail-to-rail behavior. From now, each transistor corresponds to a compound of 3 transistors with minimal channel length (40nm). Moreover it has two variables: width and multiplicity factor ($W$ and $m$).

2.2 Conventional topologies

In this section the basic differential structure that generates a rail-to-rail input stage will be shown. From this point arises the widely known drawback of these type of stages: the variation of the equivalent transconductance at the input. It modifies the gain in subsequent stages if common mode input voltage varies, besides, it makes the frequency compensation more complex, and spend more power. Later on, one of the most used techniques to solve this problem and its behavior respect to PVT variations will be presented.

Figure 2.5 presents the most basic fully-differential rail-to-rail input stage [17], which has two complementary input pairs and current mirrors on each side to add the signals in output branches. It is clear that this circuit is only the input stage because there is no gain, it is due to the diode connection at the output that ensures a permanent current flow at the output. This circuit operate as follows: each differential pair operates in an specific region of common mode depending on the type of transistors. P type operates from the lower voltage and depending on the threshold voltage will be turned off, usually after half of supply voltage. In the same way, N type transistors operate before half of supply voltage until the highest voltage.
The previous explanation can be described by three operation regions, which have different transconductances values depending on if one or both pairs are on. This behavior is described through the following equation, where $Gm$ is the total equivalent transconductance of the circuit. The ideal transconductance addition in these three regions is shown in figure 2.6 [19].

$$Gm = \begin{cases} 
  gm_p & \text{if p type pair is on (region 1)} \\
  gm_p + gm_n & \text{if both pairs are on (region 2)} \\
  gm_n & \text{if n type pair is on (region 3)} 
\end{cases}$$ \hspace{1cm} (2.2)

Another interesting behavior is obtained when input differential pairs operate in the sub-threshold region. In this particular case, the growth of $g_m$ is lineal with respect to common mode input [19]. The previous situation is presented in figure 2.7 assuming an ideal behavior, but it is very difficult to retain the input pair in this region with PVT and common mode variations. However, it is the desired behavior which also offers a high transconductance-current ratio.

Figure 2.8 presents a simulation of this circuit in the saturation region. As it can be seen, the result is so far from ideal behavior. This phenomenon is not observed in other technologies where the behavior of the circuit is close to the ideal case with good
2.2 Conventional topologies

Figure 2.6: Equivalent transconductance in an ideal stage.

Figure 2.7: Equivalent transconductance with sub-threshold operation.

definition of the three regions. But in this case the undefined region (transition region) is wider than any of the other defined regions.

The principal objective behind the use of rail-to-rail circuits is to obtain an amplifier that works without any restriction of common mode input voltage, and maximize the use of available voltage. This circuit satisfies it, but produces distortion between signals with different DC levels and other problems explained before. For these reasons it is highly desirable to obtain a full input range with constant transconductance value.
2.2.1 Dynamic compensation

Many publications are available in the literature regarding how to obtain a constant behavior of the transconductance. Most of them are based on a basic analysis of the branch current. When only one differential pair is enabled, in the output branch flows a current equivalent to $i_n$ or $i_p$, the $gm$ can be designed equal with the correct sizing to compensate $K'$ parameter (also call intrinsic gain), but in region 2 flows the addition of these two currents rises the transconductance value. Therefore compensating the current addition is the logical solution in order to obtain at the output branches a constant current value.

In the work presented in [20] a solution developed according to the analysis described above. A dynamic compensation scheme is implemented by means of the circuit shown in Figure 2.9, and works as follows: In the original circuit shown in Figure 2.5 two dummy differential pairs are connected such that they do not interfere with the signal path. Therefore, these transistors do not contribute with transconductance. However, these dummy pairs have their gates connected to the same common mode input voltage, and it subtracts current of the principal differential pair when the main pairs are enabled. This means that when only one pair is enabled the dummy pairs are disabled, but when two pairs are enabled the dummy pairs subtracts current of the main branch and reduce the transconductance value. The above solution is a better technique to compensate
transconductance than static compensation, in which constant values of current are added and subtracted to compensate the regions [17], but this only works with behaviors near to the ideal.

Figure 2.10 shown the circuit simulation results, which in the dynamic compensation eliminates the mid region in which rises the transconductance value. Apparently this is a
good solution and establishes a good transconductance behavior. A PVT simulation will be performed in order to establish whether the circuit is robust or not.

2.2.2 PVT Analysis

Figure 2.11 presents the simulation results of 45 corners in this circuit, giving as a result strong variations and distorted curves. The main concern is that the constant behavior is not achieved at most of curves. In the figure it is clearly observed two strong trends that corresponds to two temperature corners. These simulation results raise the question about why this circuit and the transconductance are so sensitive. Next, some issues associated to circuit compensation will be presented.

- Rather than other specifications such as gain or bandwidth, transconductance \( (g_m) \) is an transistor’s intrinsic parameter. Therefore, PVT variations modify the current and internal transistors parameters, modifying strongly the transconductance value.

- In some applications it suffices to guarantee a minimum or maximum value (for instance noise or gain) for a given specification. However, for other applications such as OTA-C filters and active inductors [9] a defined value in some specifications it is needed.
2.2 Conventional topologies

<table>
<thead>
<tr>
<th>Corner</th>
<th>Requirement on bias current</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max. Temperature (120°)</td>
<td>Increase</td>
</tr>
<tr>
<td>Min. Temperature (-40°)</td>
<td>Reduction</td>
</tr>
<tr>
<td>Max. Voltage (1.1 V)</td>
<td>Reduction</td>
</tr>
<tr>
<td>Min. Voltage (0.9 V)</td>
<td>Increase</td>
</tr>
<tr>
<td>slow - slow corner</td>
<td>Increase</td>
</tr>
<tr>
<td>fast - fast corner</td>
<td>Reduction</td>
</tr>
</tbody>
</table>

Table 2.1: Requirements in biasing to make a robust circuit.

- To compensate an internal parameter with minimal channel length is a difficult task. In fact, to this day there are no strategies reported in the literature for the compensation of analog blocks based on devices with minimum channel lengths.

Although it is only an example, most of the techniques used to obtain a constant $g_m$ operate in the same way and do not take into account PVT variations. It could be observed that the effect of these variations is immediately viewed in current behavior. For these reasons it is desirable to make an analysis about what is the ideal behavior in terms of current to try to compensate the variations. In table 2.1 the characteristics required over bias current to mitigate variations are shown. These required characteristics are opposite to the behavior of the circuit because of the variations, and it is assumed that is the required behavior in a compensation bias circuit.

From the previous table some particular characteristics are extracted in order to determine whether it is a good solution to try to compensate this circuit with other circuit blocks that present the opposite bias behavior. The results in voltage and process variations are positive due to its presents concordant behavior. It means that when supply voltage is lower, the current will be reduced and therefore the $G_m$ value; in the same way, when corner slow-slow happens the same effect is obtained (for the other two cases the same analysis could be made). Previous analysis means that the same control action (increase current) benefits process and voltage variations, but in the case of temperature, at the minimum value it will be presented in the circuit an increase of $G_m$, and for most of the bias circuits when temperature decreases the current decrease as well. This contrary behavior in temperature is opposite at process and voltage, for that reason the compensation of one harms the other, making of the compensation a very creative and complex process. This alternative was successfully applied in [9] to other application, but it will not be used in this work in order to explore alternative solutions applied directly over the input stage.
Based on presented simulations and analysis made about table 2.1, it is concluded that $G_m$ is a highly sensitive design variable and its wide variation cannot be compensated in a satisfactory way. For these reasons, it is necessary to study other techniques to improve circuit behavior. An interesting fact, it is that for digital circuits the incidence of the variations is smaller than in analog circuits. Apart from the widely known advantages of these types of circuits, an outstanding fact is that digital circuits in most of cases are incorporated to feedback systems, that strongly impose the desired specifications. Then, it leads to a defined output very distant from internal parameters. In this way, negative feedback appears to be a good technique to reduce the dependence on internal parameters and ideally provides a constant behavior in the presence of any variation and initial conditions.

2.3 Feedback Differential Pair

The previous section established that to obtain a robust stage entails to achieve a stable value of bias current. The external compensation could be very complex and likely increase the power consumption, therefore, the research aims to obtain a robust core of the circuit (polarization and differential pairs) because the basic circuit is biased with a simple current mirror that is very sensitive. An option is to employ another bias structure such as a cascode or a wilson current mirror. However, as mentioned before, the limit in supply voltage and compound transistors makes it difficult to employ these structures in the signal branch. Therefore, another type of solution is required. In [21] a relative novel structure was proposed to apply feedback in the polarization of a differential pair. The circuit is shown in figure 2.12, it is called the FDP and works as follows:

Inside the dashed box is the feedback structure. This is composed of a differential pair, a bias current and the transistor at the bottom provides the output. The internal differential pair is connected to the common mode voltage and ideally its current will be constant as imposed by the current source. However, this does not happen, and when common mode varies or any other parameter or variable varies (PVT, intrinsic parameters of transistors etc.), the desired current changes its value. The change in current regarding reference is sensed in the $x$ node and it saves this information. The voltage of this node is connected to the reference node closing the feedback loop and imposing an strong behavior in the internal current, now it is only necessary mirror this current outside the box, where the core circuit works with a better biasing.
Other main advantages are described below [21]:

- Common mode input range is extended even if the bias transistor of external pair enters to the triode region.

- Internal differential pair’s transconductance is more robust.

- Parameters such as CMRR, PSRR, band-width and gain will be more robust because its directly depends on input pair transconductance.

- This kind of connection makes possible to use other feedback loops in subsequent circuits.

- The new bias circuit use the two kinds of transistors, and was stated before that this structure makes the circuit more robust to cross corners.

- Using this structure, a biasing without adding transistors in the column is achieved, hence the dynamic range is not affected.

In order to verify the properties of this topology a simple simulation of differential pair and current mirrors is performed, obtaining an outstanding reduction in current variability. Given the advantages of this topology, it is quite desirable to incorporate it in a rail-to-rail stage, as it will be shown in next section.
2.3.1 Rail-to-rail input stage with FDP

In [22] a rail-to-rail stage that incorporates the FDP is proposed. Figure 2.13 presents the core of the proposed circuit, which provides \( gm \)-constant behavior including the two feedback loops that works as follows:

Transistors \( M_5, M_6, M_{12} \) and \( M_{13} \) are the input differential pairs, \( M_3, M_4, M_{10} \) and \( M_{11} \) are the differential pairs that makes the feedback over the main pairs. Besides the previous, two additional pairs formed by \( M_7, M_8, M_{14} \) and \( M_{15} \) are incorporated, whose
2.3 Feedback Differential Pair

Figure 2.14: $g_m$ constant behavior with drastic feedback.

function is impose an strong behavior over the main complementary differential pair. The behavior of this circuit provides a soft curve like figure 2.10 (saturation transistors), but sizing properly the transistors in the two feedback loops, an abrupt behavior can be forced. Also, if the input differential pairs operates in the sub-threshold region, a linear characteristic in the transconductance transition is obtained.

This constitutes the first notable contribution of this work, since the strong feedback takes advantage of sub-threshold operation to provide the most close performance to an ideal behavior. The improved behavior can be seen in figure 2.14 and the circuit operation is described below:

Suppose that the input common mode voltage is minimum, then, all N type differential pairs are in the cut-off region and the P type transistors are in sub-threshold region, $M_{14}$, $M_{15}$ and $M_{18}$ provides the DC path to the ideal current source. Therefore, $M_{refp}$ is off and this behavior produces that the N part of the circuit be disabled by two mechanism as follow: the low input common mode voltage and the lack of bias current due to $M_{refp}$ is off. As the common mode raises, the N type differential pair will start to turn on, but the feedback of P type bias differential pair causes $M_{14}$, $M_{15}$ and $M_{18}$ to remain enabled even if $M_{18}$ reaches the triode region. For this reason and despite the input common mode value it is not enough to turn on N transistors, they do not have bias current and remain off. As the input common mode voltage is about half of the supply voltage, the previous
situation is untenable, and due to the high loop gain the N type differential pairs suddenly turn on, immediately, $M_7$, $M_8$ and $M_9$ absorb all the current of the source, turning off $M_{refn}$ and disabling all P type differential pairs. It is worth noting that all differential pairs and biasing are designed with the same current capacity.

The previous behavior only can be achieved by employing the FDP circuit, designing with high loop gain the feedback loops and with sub-threshold operation for the input differential pairs. A PVT simulation is performed in order to establish if the previous techniques are effective to reduce the transconductance variations. Figure 2.15 shows the circuit PVT simulation. Although the results are not ideal, some interesting details are observed in order to obtain a better performance.

The circuit simulation demonstrated that a big portion of the curves remain compensated (rather than dynamical compensation), besides the effect of variations tend to be reflected in the value of common mode voltage at which switching occurs. The described behavior is highly positive, because it is desirable that the effect of variations change the switching point instead of the transconductance addition and it does not matter if the switching occurs at the beginning or the end while the addition will be constant.
2.4 Improved and Compensated FDP-R2R Stage

In this section a new rail-to-rail input stage based on topology proposed in [22] will be discussed. This topology does not have gain, and is compensated against PVT variations. The lack of gain and full input swing characteristic suggest that this topology can be used like input stage in any amplifier without affecting the compensation scheme. Also, it is the first work reported with this characteristics in nanometer and SOI technologies fulfilling all model and fabrication restrictions.

Figure 2.16 shows the proposed architecture that works as follows: the circuit has the same core and drastic feedback design explained previously, but the current mirrors were improved because they are the input of the desired feedback system. For these reasons simulations were performed with different current mirror structures (cascode, wilson and high compliance amongst others), considering that the connection must allow for feedback. The best performance was achieved by the improved wilson current mirror, other feedback structure. The change in current mirrors is possible because the FDP structure moves the bias circuit to an independent branch which is not part of the signal path and therefore input dynamic range and operation point of input branches is not affected.

Besides the former modification, previous sections identified that the behavior of temperature is opposite respect to process and voltage variations For this reason two current mirrors are incorporated at the output to add the currents. These current mirrors have opposite behavior in temperature with respect to the core of the circuit, enabling them to compensate for each other.

Figure 2.17 presents the dynamic of the compensated circuit, whose transconductance behavior is the desired and difficult to obtain in nanometer technologies. Figure 2.18 presents the PV simulations that show a totally improved behavior with respect to the rest of circuits. The total variations are concentrated in only 6 switching points and the transconductance remains constant for the most of curves. Figure 2.19 shows the frequency response, where only two decibels separate the worst cases in a PVT simulation. Finally, figure 2.20 presents the variations of output the common mode level with regard to input common mode level. This is a very important concern in order to integrate the stage with each other. Another advantage is that the output common mode voltage is well defined and a CMFB circuit is not necessary. The next chapter will show how diode connection is a robust connection. Additionally, the transistors connected at the output are not compound transistors, but single transistors in order to improve the output swing
Figure 2.16: Improved and Compensated FDP Feedback Rail-to-Rail Input Stage.
and to reduce the change of the $Gm$ value at the output. Finally, table 2.2 details the characteristics of design, where all the transistors are $aut$ type, the channel length is restricted to 40 nm, and the width is the nominal value for each type of transistor.
2.4.1 Results and comparison with other works

In this section the partial results of this work are compared with other works, to show the improvement achieved with the proposal. Table 2.3 shows the comparison with the best 4 papers found about $gm$ compensation.
2.4 Improved and Compensated FDP-R2R Stage

<table>
<thead>
<tr>
<th>Transistors m</th>
<th>Transistors m</th>
</tr>
</thead>
<tbody>
<tr>
<td>M_{1-4,17,18}</td>
<td>30</td>
</tr>
<tr>
<td>M_{14,15}</td>
<td>10</td>
</tr>
<tr>
<td>M_{8,11}</td>
<td>15</td>
</tr>
<tr>
<td>M_{25-28}</td>
<td>30</td>
</tr>
<tr>
<td>M_{7,12}</td>
<td>20</td>
</tr>
<tr>
<td>M_{19,24}</td>
<td>13</td>
</tr>
</tbody>
</table>

*Not compound transistors.

Table 2.2: Input stage design characteristics.

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>This work</th>
<th>[23]</th>
<th>[24]</th>
<th>[25]</th>
<th>[26]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Process [µm]</td>
<td>0.045</td>
<td>0.35</td>
<td>0.35</td>
<td>0.18</td>
<td>0.35</td>
</tr>
<tr>
<td>V_{dd} [V]</td>
<td>1</td>
<td>3</td>
<td>1.5</td>
<td>1.8</td>
<td>3</td>
</tr>
<tr>
<td>g_{m0} [mA/V]</td>
<td>1.55</td>
<td>1.9</td>
<td>0.043</td>
<td>0.175</td>
<td>0.782</td>
</tr>
<tr>
<td>g_{m} Variation [%]</td>
<td>4.1</td>
<td>2.64</td>
<td>6.8</td>
<td>4</td>
<td>0.4</td>
</tr>
<tr>
<td>Robust to</td>
<td>PVT</td>
<td>-</td>
<td>-</td>
<td>V</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 2.3: Comparison with related works.

Figure 2.21: Gain vs. Common mode input level.

All the works reported with g_{m} constant behavior were made in technologies in the upper 0.18 µm, still suitable for analog design. The results reported by [23] correspond to the best simulation point obtained among different bias current, but other biasing points achieve a variation closer to 5%. In [26] the best result in terms of variation is presented. Here, the circuit employs different amplifiers for input stage, which is a very complex so-
lution that spend a lot of area and power consume for the input stage. The works [24,25] present low values for \( g_m \), and do not seem to be the ideal choice for amplifiers. This work is unique in the area, PVT compensated with a useful transconductance value (taking into account transistor behavior and compound transistors), and the lower supply voltage.

Finally, the maximum variation of gain in frequency response over the 45 corners corresponds to \( \pm 0.84 \) dB, where 80\% of the curves have a variation less than half of the total variation. The maximum variation in gain with different common mode values is \( \pm 0.98 \) dB as shown in figure 2.21. The value of bias current is 250 \( \mu \)A, and the total power consumption is 770 \( \mu \)W. The next chapter will show how to obtain a useful gain robust to PVT variations.
In this chapter will be designed the gain structure that follows the input stage designed previously. This chapter shows the proposed technique in order to avoid the low frequency poles and zeros. Then, some robustness considerations and an analysis over some architectures for obtaining high gain will be explained. The fully differential operation of the topology requires a CMFB circuit, therefore, a discussion about this type of circuits and its incidence over PVT variations will be detailed. Finally, a comparison with related works will be made.

3.1 Disadvantages For High Gain

The robust design for analog circuits in nanometer technologies implies splitting circuit operation and solving the drawbacks of each stage, since in many cases only one source of strong variability can make useless the circuit. For this reason, the design of gain circuit will be made stage by stage applying some robustness considerations.

One of the most important concerns in amplifiers using nanometer technologies is to obtain useful gain, due to most of the circuits that employ amplifiers works based in ideal specifications like infinite gain (depending of application could be more than 80 or 100 dB). Theoretically, it exist a higher limit that is outside of technology scope (for common topologies). This fact was presented in chapter 1, where the most simple configuration was able to obtain only 21 dB. This gain value is at least 9 times minor than the gain obtained with micrometer technology (volts units). Whether it is the difference with only one stage, it can be anticipated that the difference will grow up using more stages.
Thus, obtaining a gain close to 60 dB requires at least three stages, since cascode topologies are not suitable in this type of technology due to the low supply voltage value and the low frequency of poles and zeros as will be shown later. Previous works show that the development of topologies with relative high gain has several problems in frequency compensation, even with two stages. To solve this problem, a frequency compensation technique for an amplifier in 65 nm technology was proposed in [13], whereas in [3] was probed that to compensate an amplifier with two stages in current technologies is required more than one compensation scheme. Then, the use of more than two stages does not seem to be the best choice.

Other problem is the extremely high channel modulation effect, which is solved like was shown in chapter 2. Next, it will be presented a new drawback of technology itself, which make more complex the circuit compensation and modifies the amplifier’s flat-band gain.

### 3.1.1 Flat-Band gain’s variation

In [3] was designed an amplifier in current technology, one of the most interesting discoveries was the low frequency poles and zeros in the amplifier’s pass-band. This phenomenon is totally new and does not exist papers about its causes or possible solutions. In this document, this behavior will be detailed in a deepest way, trying to establish the possible causes, the main consequences and restrictions. In the same way, over this section will be factually determined the origin of this problem, how it becomes more observable, under which circuit conditions is more dangerous, and finally, it will be formulated and hypothesis about electrical causes of this problem. Another contribution of this work, is to propose a solution for SOI technology, in order to avoid this undesirable behavior employing different types of transistors.

Figure 3.1 shows the frequency response of the amplifier in figure 3.2, as it can be seen, the gain has a sudden increase in its value on the flat-band and the phase behavior confirm that this increase is generated because first appears a zero and very close a pole. In some cases the pole can appear and afterwards the zero, generating a decrease in gain. Despite of these simulations it raises the question about why it was not observed in the input stage simulation. To answer this question is necessary obtain more information through simulations, it to define if the location of poles and zeros have dependence on other circuit characteristics.
3.1 Disadvantages For High Gain

Figure 3.1: Frequency response of one stage amplifier.

![Graph showing frequency response of a one stage amplifier.]

Figure 3.2: Basic configuration of a one stage amplifier.

![Diagram of a one stage amplifier configuration.]

Figure 3.3 show the frequency response magnitude of two different amplifiers. The first one is a two stage amplifier whose response is plotted in dotted line (basic single structure of figure 3.2 and common source) and the second is an standard folded cascode structure. From the graphic it is so clear that poles and zeros location has an strong dependency on gain, besides the increment of gain increases the distance between them.
Another observation is that the separation increases regarding connexion complexity, it is due to folded structure has similar gain that the two stages amplifier and shows a worst behavior. The last fact is other reason for not to use cascode topologies, because the flat-band gain’s variation becomes more pronounced.

Other interesting topic is to establish if the compound transistors can reduce the distance between the pole and zero. Therefore, some simulations were made without compound transistors. The obtained result is a marked increase of the distance between pole and zero (due to the result of these simulation is easy to understand such as others presented, the figure will not be displayed). The effect of compound transistors is clear to reduce the distance between the pole and zero, consequently, the change in gain variation value is reduced close to the half with respect to single transistors. Through previous simulations is possible to determine why this behavior was not be observed in the input stage: the input stage has not gain and use compound transistors, for these reasons the flat-band gain’s variation could not be seen. Hence, the input stage is robust with respect to this drawback and does not require any change. Additionally, it is another reason to keep using compound transistors in the circuit.

Unlike the input stage, the gain stage will suffer from flat-band gain’s variation due to the pretended high gain, and the use of compound transistors is not enough to solve
3.1 Disadvantages For High Gain

Figure 3.4: Variation of poles and zeros location with respect to PVT variations.

it. Therefore, it is necessary to perform more simulations and establish some criteria that enable identifying causes and formulate solutions. A PVT simulation is performed, obtaining a variation for the location and distance of the pole and zero. Specially it changes with regard to temperature and process corners such as figure 3.4 shows, in which are plotted the two extreme temperature cases and the fast-fast corner. It suggests that the location depends on the internal parameters modified by process or temperature.

3.1.1.1 Possible causes and an effective solution

Since this problem directly harms the gain specification and depending on location could be a source of instability for the system, a solution is needed in order to continue with the design process. For this reason is necessary to make an analysis in order to provide a viable solution.

It is very important to highlight the fact that this phenomenon does not occur in CMOS technology, accordingly, it is a behavior induced by technology. The main differences with CMOS are the insulator layer and the absence of body terminal. The simulation with compound transistors shows a reduction in the gain variation, which suggest that the SCE have a direct impact on the phenomena. The PVT simulations show that the location of pole and zero depends on transistors properties and conditions in the
circuit. It means that is possible to modify the location with design variables, for instance biasing. Also, it was observed that increasing the complexity of the structures, the effect becomes more negative.

The poles or zeros in electronics circuits are commonly associated with capacitances in direct or feedback paths. The explanation provided by this work is consistent with the observations: this phenomena is attributed to the high leakage currents in transistor gate and the charge accumulation in body region without a fixed potential. In this conditions multiple paths are created in specific regions of the circuit generating poles and zeros. This affirmation makes sense because the transistors models has the way to simulate both effects (leakage and trapped charge), the charge accumulation is due to the insulator layer and the potential into the body section of transistors is undefined. In the same way, the leakage currents are an important part of SCE and the use of compound transistors reduces its incidence. Consequently, the amount of leakage and trapped charge varies with transistors parameters and conditions. Finally, in the previous paragraph was mentioned that increasing system complexity (also gain) raises the negative effects. This is related to the load of input differential pair. To achieve more gain it is necessary more interconnections and incorporate more transistors, this modifies the dynamic of gate leakage and trapped charge, specially in diode connection transistors.

Although the attributed causes could not be demonstrate mathematically or physically, the solution is consistent with the previous analysis as follows: in order to provide a path for releasing charge and a portion of the leakage current flow, another type of transistor must be used. Placing body-contact transistors in the load of the input differential pair can be defined the body potential and create a path to set free the trapped charge. This solution was tested with different topologies obtaining the desired flat-band performance. Figure 3.5 shows the improved behavior of the circuit in figure 3.2, where the phase response avoids the low frequency gain variation.

### 3.2 Robust Design

There are many kinds of amplifiers and depending on the desired specifications should be selected the topology, but in most of cases it is not considered if the circuit is robust and can provide the same performance under different conditions. In this section some concepts proposed in [27] and other related concepts to determine when an amplifier is a robust circuit will be explored.
3.2 Robust Design

Figure 3.5: Improved frequency response.

Figure 3.6: Basic three stages amplifier.

Figure 3.6 shows a three stage amplifier composed by a differential pair and two common source stages. This kind of configurations are widely studied with academic purposes and is useful to explain how some topologies are more sensitive to variations. The voltage in p node ($V_p$) is well defined by diode connection, whereas $V_n$ voltage also is defined due to symmetry of differential pair and try to follow $V_p$ value. Because of $V_n$ value is estab-
lished, the current of second branch is imposed by the gate voltage of its two transistors, but the voltage \( V_b \) has a dynamic behavior and it is not controlled by any connection or device, therefore neither current nor voltage are well defined in the output branch and the most slight variation in any stage causes changes in biasing. Accordingly, the circuit is not robust, the variations in current at the output modify specifications such as slew rate, band-width and gain among others. The variation of the voltage for instance modifies the output common mode and operation point. This kind of circuits or biasing generate outputs such as was showed in figure 1.10.

Figure 3.7 shows another three stages configuration. Following the previous analysis could be observed that all the \( V_p \) voltages are well defined. Consequently, the output branch current is defined achieving a relative robust structure. It is interesting that this analysis agrees with the observations drawn in spite of simulations made by [3, 9], about the considerations to obtain robust structures for this technology. Also, it has relationship with the output common mode variations for fully differential circuits, in which case, if it has transistors with diode connection at the output, the CMFB circuit is not needed. In short, the differential pair is one of the most solid structures due to its symmetry, and the diode connections are useful between stages to provide stability in the circuit. Moreover, the structure for the amplifier must follow the concepts presented above in order to obtain a robust structure. Clearly these are not the only considerations that are needed to obtain a functional circuit, but must be take into account to eliminate possible sources of variation. Others widely known characteristics that make robust a design are:

- Cross signal paths [17]: In fully differential topologies it is possible to cross the
signal paths, it means that if the circuit is divided in left and right parts, the signal of one side could be connected to the other one. This improves the dynamic of the circuit with respect to tail current and makes that both signals have the same path to the output (suffering from the same distortion and noise among others). An example could be seen in figure 3.9.

- N and P routes: In biasing and signal path are suitable makes that the current flows through both type of transistors, it is in order to make that the current flow always be affected for N and P variations. It due to inside the transistors a lot of behaviors are opposite, therefore, the variations could be compensated [3, 9].

- Robust biasing: With the low value of supply voltage, it is possible that the biasing transistors does not remain in saturation. Previous chapter shows that a robust biasing could improve the behavior and reduce the incidence of variations over circuit performance.

### 3.2.1 Structures for high gain

Based on the discussion presented in previous chapters, it is looking for a two stage amplifier and the cascode topologies are not allowed. It is due to the low supply voltage, the extensive use of compound transistors and low frequency gain variation. Next, some reported and widely know structures will be shown in order to establish if they are suitable for high gain and fulfill the robustness criteria and design considerations.

Figure 3.8 shows an improved configuration of the current mirror Operational Transconductance Amplifier (OTA). In the original configuration the current is mirroring with a relationship different than the unity “increasing the gain”. But no increase is achieved because the output resistance and transconductance have opposite behavior regarding current. Therefore, the increase in one specification is compensated with the decrease in the other. With the addition of $M_3$ and $M_4$ the current of differential pair and output branch can be made independent, it achieving a significant increase for gain using one stage only. The relation 3.1 shows the increase in the gain ($K$) compared with common topologies. The $K$ factor is achieved with the difference between the input differential pair current and the output branch current, its value usually is 2 or 3 because an excess in this value harms the phase margin specification significantly.

$$A = K gm_{\text{pair}} (r_{05}/r_{010})$$  \hspace{1cm} (3.1)
Apparently this architecture provides a lot of benefits, improve the gain specification, the frequency response and time response. In order to verify these assumptions some simulations were performed. With the proper sizing of $M_3$ and $M_4$ the improvement for gain is close to three times (V/V units) with respect to common topologies.

A two stage amplifier with gm addition and cross paths was reported in [17], figure 3.9. The gain expression for this circuit is shown in equation 3.2. As it can be observed, this configuration can double the gain regarding the basic two stage amplifier (it was simulated and verified). Moreover, it uses cross and complementary paths.

$$A = gm_{\text{pair}}(r_{0_{2,3}}/r_{0_{7,8}})(gm_{1,4} + gm_{5,6})(r_{0_{1,4}}/r_{0_{9,13}})$$

The previous two topologies improve the gain and have in common that the load transistors and biasing does not meet with the considerations made to robustness. Also, the biasing for differential pair’s load through a fixed voltage it is not desirable, since it is a source of strong variability as shown this work and in [3, 9], even if the bias voltage is an ideal voltage source. Consequently, the performed PVT simulation for each topology shows a high variation in the frequency response (including CMFB circuit). Figure 3.10 shows the frequency response of the mirror OTA with current shunt, where is observed an increase of 6 dB. Also, the PVT simulation results show the dreadful behavior with respect to variations. The previous results indicate the importance of robustness con-
3.2 Robust Design

Figure 3.9: $g_m$ addition two stages amplifier.

Figure 3.10: Shunt amplifier PVT Simulation.

siderations and that all the suggestions must be taken into account to obtain a robust performance.

An important fact drawn from previous simulations it was the elimination of the low frequency gain variation owing to the usage of body-contact transistors, even in presence of PVT variations. In [3] was proposed an architecture to achieve 54 dB and robust behavior even in presence of PVT variations. Figure 3.11 shows that the circuit incorporates
transconductance addition and the structure meets in almost all connections with the robust considerations made previously. Despite this, the gain specification is not higher than 60 dB yet, which is the minimal gain desired to this work.

To define the best choice to achieve a robust amplifier with high gain is a hard work, therefore, the most important information to achieve it will be described next: conventional amplifiers usually have only one transconductance that spreads through the circuit and high impedance nodes that depends on the number of stages. However, the circuits of figures 3.9 and 3.11 have one transconductance addition and two gain nodes. Depending on connections to add the transconductances the circuit will be robust or not, it follows that to obtain the gain specification, this work will propose a two stages amplifier with two transconductance additions (to achieve double gain with respect to previous works) meeting with all the robustness considerations.

3.3 One stage proposed architecture

To obtain a two stages and two \( gm \) additions amplifier, it is clear that must be done one addition per stage. Modifying some connections in the input load for the circuit in figure 3.9, this topology can be converted in one stage with one transconductance addition. Thus, the bias circuit is improved through the FDP in order to obtain all the benefits previously described. The final topology for one stage amplifier is show in the figure 3.12.
To design it the next considerations were taken into account:

- N type input pair is selected according to the output common mode level of previous stage ($\approx 0.75 \, \text{V}$).

- With the change in connections of pair load, all the circuit fulfill with the robustness considerations explained in previous sections, additionally, the current at the output branch it is established by two different diode connections of different type (N/P).

- The circuit has N and P signal and bias paths.

- The cross signal paths provide a good dynamic between differential signals at the output (class-AB output) [17]. Moreover, the signal on each side will be affected equally by the undesirable effects of both sides. For example, in case of temperature gradients or wrong layout location, the circuit could be more affected in one side than the other, unbalancing the circuit. Due to the cross paths, the differential operation try to eliminate these variations.

- Input differential pair is designed in sub-threshold region to obtain the maximum gain. In addition, this operation region has less variability than the others accordingly to $gm/i_d$ curves.

- An increase in gain is obtained according to the equation 3.3.
The use of compound transistors improves the circuit performance and robustness.

FDP structure allows using a better bias circuit without reducing the input dynamic range. Also, it provides all the benefits explained in chapter 2.

Transistors $M_{1-6}$ are body-contact (A type) in order to avoid the low frequency gain variation. This selection was made taking into account that $M_{2,3,5,6}$ are the load of input differential pair and $M_{1,4}$ are current mirrors.

To achieve the desired gain and robustness the number of branches is increased with respect to conventional topologies. Consequently, this increase in current paths raises the power consumption.

$$A = (gm_{par} + gm_{5,6})(r_{0_{1,4}}/r_{0_{9,13}})$$

Accordingly with the results showed at the end of chapter one, a minimum gain of 60 dB was proposed, where each stage provides the same gain. Therefore each stage has to achieve 32 V/V in the worst case. In frequency response it is expected to obtain close to 400 MHz in Gain-Bandwidth Product (GBW), as well a phase margin between 55° and 70° with a load capacitance of 0.3 pF. The previous specifications are defined in order to compare the results with most of reported works in the state of the art.

### 3.3.1 Common mode feedback circuit

One important concern in fully differential circuits is the CMFB circuit, because its function makes possible to obtain a defined common mode voltage value at the output. A large number of circuits can make this task and most of them could be classified in four groups:

- Resistors based: In this kind of circuits the sense circuit is made with resistors, but the value must be high to reduce the load effect at output nodes. On the other hand, resistors with high values spend a lot of area and its behavior is significantly affected by temperature. Also, it has problems with mismatch and temperature gradients. In some cases are employed transistors like buffers to separate the resistors from the output node, but these transistors easily can get out from saturation region limiting the output swing and introducing distortion.

- Triode region based: Using transistors like resistors is another option, but with the dynamic of the circuit the resistors value change. This proposal also suffer from
the same disadvantages with respect to distortion and reduce the available dynamic range. On the other hand, the PVT variations significantly harms this type of circuits, making it not robust.

- Differential pair based: This one is widely employed due to the gates of transistors, which are sensing, do not load the output. Also, this circuit has symmetry and the control action is very effective. But the main drawback is that this type of circuits reduces the output dynamic range and the PVT variations harm its performance.

- Bulk based: If the sensing circuit use the bulk terminal of transistors the output nodes are not loaded and the dynamic range is not affected. Moreover, some configurations shows that the distortion does not increased and it is a good choice to low voltage circuits [28]. However, any estimation had been done about how the PVT variations modify its behavior and its viability in SOI technology, for these reasons some simulations were conducted and the control action is not effective with the current transistors.

- Switched Capacitor (SC) based: It is the choice in discrete time applications. It is because can operate at high velocities, does not load the output nodes, the PVT variations do not affect its performance significantly and do not harm the dynamic range. Despite this benefits, this circuit is affected by phenomena associated to charge such as clock feedthrough, noise coupled at the output and charge injection among others.

The amplifier requirements impose that dynamic range can not be decreased, the load at the output nodes is not suitable for a proper operation and requires big resistors that spend a lot of area with high temperature variability. The result of previous analysis only consider the bulk and SC based as viable solutions.

Despite the previous analysis, the last three detailed options were implemented and simulated. The differential pair based CMFB option shows good behavior under typical conditions, but with PVT variations the desired operation point change. The body-contact transistors does not achieve the desired control action to this circuit. Finally, the SC option was successfully implemented and applied, it showing robustness in presence of PVT variations. The previous behavior is explained because the capacitors are not affected by variations and the transistors operates like switches. Therefore, the variations does not affect the behavior significantly as it will be show in simulation section. Figure 3.13 shows the SC-CMFB circuit implemented. To design this circuit the next characteristics were taken into account:
Figure 3.13: Switched capacitor common mode feedback circuit.

- All the switches are transmission gates in order to reduce effects like clock feedthrough, decrease the on resistance equivalent and also controls the charge injection phenomenon.

- In transmission gates is required complementary clock without overlapping phases to reduce charge injection.

- The regular \textit{vth} transistors were selected to implement the switches because they are the smallest transistors with the lowest threshold voltage. Additionally, the switches were implemented with compound transistors to reduce the coupled noise at the output.

### 3.3.2 Simulation

Figure 3.14 shows the frequency response of the amplifier, where a gain of 32.6 dB and a GBW of 405 MHz were achieved ($C_L=1$ pF), the phase margin obtained was 63.1°. The achieved gain is an important result, since it is close to three times the estimated gain obtained by a common one stage, and it validates the considerations that were made previously. Figure 3.15 shows the PVT simulation, where all the samples are consistent in gain and phase showing a robust behavior in the circuit. On the other hand, none low frequency gain variation is observed. The transistors and circuit characteristics are summarized at the end of this chapter with the whole gain stage.

Figure 3.16 shows the response of CMFB circuit in the most extreme cases (with initial conditions of 0 and 1 volt) and regardless this conditions the feedback system always reach the desired output common mode value. Figure 3.17 shown the action of CMFB circuit under PVT variations, the results verifies that this scheme works properly under this type of variations and also reduce its incidence in the circuit. At the top of the figure
3.3 One stage proposed architecture

Figure 3.14: Frequency response of designed one stage amplifier.

Figure 3.15: PVT variations over designed circuit.

is shown how in the worst case (extreme initial condition and PVT variations) the output common mode voltage reaches the desired value and at the bottom is shown how the maximum variation between the extreme cases is reduced by the action of CMFB circuit. Other schemes have higher variations which does not be reduced along time.
The total power consumption is 1.7 mW, due to the high load capacitance and the current required to obtain the desired GBW. Another interesting feature is that the current reference value could be changed in order to reduce the power consumption, increasing gain and decreasing the GBW, foregoing retaining robustness in behavior. The power consumption, GBW and phase margin are not definitive, because with the second stage
3.4 Proposed architecture for two stages

The results of previous section indicate that all the considerations were correct and the second stage must preserve the same considerations. In order to accomplish this, it is enough with expand the robustness considerations at the subsequent stages as follows: it is needed that the next branch has not a high impedance node because the output in previous stage has one and was seen that this kind of connections are not robust; also, this branch has to split the signal to make a second addition. Thus, another branch is required. Finally it is required an output branch to provide gain and add the signals. Figure 3.18 shows one side of the second branch that operates in the same way as first stage. Equation 3.4 show the expected gain for two stages employing the double transconductance addition (the subscripts are accordingly with the scheme at the end of this chapter). Next, it will be detailed the compensation scheme.

\[
A = (gm_{51,54} + gm_{46,48})(r_{037,41}/r_{058,63})(gm_{45,49} + gm_{44,50})(r_{035,43}/r_{055,66}) \tag{3.4}
\]
### 3.4.1 Compensation

Previous works indicate that compensating amplifiers with excess of gain and high complexity of poles and zeros is not a trivial task, even when only two stages are used. The traditional compensation schemes like miller and indirect work properly while the gain value does not exceed the “nominal conditions”, it means that if the nominal gain for two stages in a specific technology is 70 dB and the circuit develops 90 dB, the difference makes the compensation of the circuit more complex or the specifications over capacitors, resistors and transistors will be significantly high in area or performance. As it was shown in chapter 1, in [3] a combination of the two mentioned compensation schemes was necessary, in [13] a variation of indirect compensation (*self-cascode compensation*) is proposed; both works in nanometer technologies. Some modifications over miller capacitances involve the use of transistors to make current or voltage buffers, but the additional devices incorporates sources of variability with respect to PVT variations.

\[ gm_2 R_m > 1 \]  \hspace{1cm} (3.5)

In this work is necessary employ the two traditional schemes in order to meet with the frequency specifications employing the minimum quantity of compensation capacitance. The miller network is connected between the high impedance nodes, in accordance with the restriction 3.5, to locate the zero in the left semi-plane. In addition, indirect compensation must be connected in a low impedance node, in this case the drain of \( M_{56} \) and \( M_{65} \) which have diode connection. Figure 3.21 shows the complete circuit including the compensation scheme. All the circuit is biased with the FDP and the CMFB circuit is connected between the output nodes and the gates of \( M_{60,91} \).

### 3.5 Simulation and Final Specifications

Figure 3.19 shows the frequency response of the circuit in figure 3.21. The gain achieved is 67 dB with 413 MHz in cut-off frequency (\( C_L = 300 \) fF), the phase margin is 54° and the total power consumption is 2 mW with 200 \( \mu \)W for bias current. The obtained result is very important because it demonstrates that is possible to obtain useful gain with only two stages without cascode topologies in nanometer technologies. Also, the obtained value is in the same range that the obtained by common topologies in micrometer technologies. Figure 3.20 shows the PVT simulation results where a gain of 67 dB with a maximum variation of +/-5 dB was obtained. For all cases the phase margin is at least 50°. Despite it was obtained high gain and robust behavior, any of the other specifications (such as
GBW or slew rate) were significantly affected with respect to the result found in the state of the art. It will be observed in table 3.2.

Table 3.1 shows the circuit characteristics, where the bigger transistor is only 26 µm on equivalent width. The body-contact transistors were used in the same way that pre-
Addition and Proper Biasing for Gain Stage

Transistors | m | Transistors | m | Compensation
---|---|---|---|---
$M_{35,37,41,43}$ | 13 | $M_{36,42,44,50}$ | 16 | $C_{mr}=1$ pF
$M_{38,40,46,48}$ | 20 | $M_{39}$ | 10 | $R_{mr}=520$ Ω
$M_{56,65}$ | 16 | $M_{47}$ | 25 | $C_{mr}=450$ fF
$M_{52,53}$ | 4 | $M_{45,49,51,54}$ | 20 | $C_{ml}=1$ pF
$M_{57,64}$ | 8 | $M_{55,58,63,66}$ | 12 | $R_{ml}=520$ Ω
$M_{59,62}$ | 20 | $M_{60,61}$ | 5 | $C_{ml}=450$ fF

*Body-contact transistors.

Table 3.1: Gain stage design characteristics.

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>This work</th>
<th>[3]</th>
<th>[12]</th>
<th>[12]</th>
<th>[13]</th>
<th>[14]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Process [nm]</td>
<td>45</td>
<td>45</td>
<td>90</td>
<td>90</td>
<td>65</td>
<td>90</td>
</tr>
<tr>
<td>$V_{dd}$ [V]</td>
<td>1</td>
<td>1.3</td>
<td>–</td>
<td>–</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Gain [dB]</td>
<td>67</td>
<td>53.7</td>
<td>52</td>
<td>65.66</td>
<td>56</td>
<td>69.6</td>
</tr>
<tr>
<td>GBW [GHz]</td>
<td>0.41</td>
<td>0.57</td>
<td>1</td>
<td>0.54</td>
<td>0.45</td>
<td>0.41</td>
</tr>
<tr>
<td>PM [°]</td>
<td>54</td>
<td>74.9</td>
<td>47.4</td>
<td>–</td>
<td>77</td>
<td>57.3</td>
</tr>
<tr>
<td>$C_{L}$ [pF]</td>
<td>0.2</td>
<td>0.2</td>
<td>–</td>
<td>–</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Power [mW]</td>
<td>2</td>
<td>1.35</td>
<td>–</td>
<td>–</td>
<td>1.6</td>
<td>2.1</td>
</tr>
<tr>
<td>Slew rate [V/µs]</td>
<td>300</td>
<td>–</td>
<td>697.53</td>
<td>556.42</td>
<td>60</td>
<td>130</td>
</tr>
<tr>
<td>Output range [$V_{pp}$]</td>
<td>1.4</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>0.56</td>
<td>1.2</td>
</tr>
<tr>
<td>Robust to</td>
<td>PVT</td>
<td>PVT</td>
<td>–</td>
<td>–</td>
<td>PT</td>
<td>–</td>
</tr>
</tbody>
</table>

Table 3.2: Comparison with related works.

The total compensation capacitance in each side is 1.45 pF and the total resistance is 520 Ω. Table 3.2 shows a comparison with related works. The obtained gain is the second higher among all works. It is very close to the maximum gain which is obtained with two stages and folded cascode structure in a 90 nm CMOS technology. The specifications of this work are very similar to [12] and [14], but the cited works employ cascode structures, which offers better performance in gain and frequency response. Besides, the technology employed in these works has the double minimal size in channel length and does not have restrictions in transistors sizing.

The band-width obtained is in the same range as the other works, therefore, an improvement in gain specification was achieved without affect significantly this specification. It is clear that all the achieved benefits in gain and robustness increase the power consumption with respect to the technology dimensions and supply voltage, but all the transistors can drive properly the designed current and the total consumption is in the same range that all the related works. The specifications and the fully characterization will be detailed in the next chapter over the whole circuit, which incorporates the designed rail-to-rail input and gain stage.
Figure 3.21: Proposed architecture to robust double $gm$ addition.
Chapter 2 and 3 demonstrated new proposals on how to obtain a robust rail-to-rail input and gain stage. For the rail-to-rail input stage was proposed that this stage can be easily integrated with any other gain stage, therefore, in this chapter the designed stages will be integrated as an OTA. In addition, the amplifier will be fully characterized detailing how some measurements were made, in order to establish if the design considerations were appropriate and does not harm other specifications. PVT simulations will be perform over different specifications in order to verify the circuit’s robustness.

4.1 Design Changes

The coupled circuit has a slightly change in the circuit behavior. For the specifications shown previously, only the compensation scheme must be modified, because the amplifier’s gain decreases adding the rail-to-rail input stage, therefore the compensation capacitances must be reduced to maintain a good phase margin and does not harm the GBW specification. On the other hand, the floating body transistors introduce several negative effects on the transistor parameters, which change along time introducing distortion in analog signals. Also, the wide use of compound transistors harms the output range, for these reasons some modifications will be done in the transistors connected at the output in each gain stage, in order to reduce the Total Harmonic Distortion (THD) over the output range.

In this type of technology the designer must be carefully with the current that the devices can drive properly. The technology documentation shows some measurements over fabricated transistors, which show that single devices can drive more than 600 $\mu A$ and
4.2 Characterization

This section shows the main measurements over the OTA circuit, in which some require details as to how the measurements were taken due to differential operation produces ideal results for some specifications. For this reason monte-carlo simulation is needed in order to validate the results.

4.2.1 Frequency response

Figure 4.1 shows the amplifier’s frequency response, in this simulation a minor gain and GBW were expected due to the addition of input stage attenuate the signal and incorporates more poles in frequency response. However, the decrease in gain allows for the reduction in the capacitances value in the compensation scheme. The new values are $C_{in} = 400fF$, $C_m = 600fF$ and $R_m = 800\Omega$. The obtained gain is 60 dB, which is the desired value for typical conditions, the GBW is 350 MHz and the phase margin is 53°.

Figure 4.2 shows the PVT simulation, which is very positive because the gain variations are minimal. The worst case for the 45 corners is so close to the typical case, and the best case is far better than the nominal case. The previous situation indicates that the performance will likely be better rather than worse. Table 4.2 summarize the frequency response performance.

**Table 4.2**: OTA design characteristics.

<table>
<thead>
<tr>
<th>Transistors</th>
<th>m</th>
<th>Transistors</th>
<th>m</th>
<th>Transistors</th>
<th>m</th>
</tr>
</thead>
<tbody>
<tr>
<td>$M_{1-4,17,18,29-32}$</td>
<td>30</td>
<td>$M_{9,10,21,22}$</td>
<td>24</td>
<td>$M_{37,41}$ **</td>
<td>13</td>
</tr>
<tr>
<td>$M_{14,15,39}$</td>
<td>10</td>
<td>$M_{20,23}$</td>
<td>14</td>
<td>$M_{19,24}$</td>
<td>13</td>
</tr>
<tr>
<td>$M_{8,11}$</td>
<td>15</td>
<td>$M_{13}$</td>
<td>16</td>
<td>$M_{16}$</td>
<td>37</td>
</tr>
<tr>
<td>$M_{25-28}$ *</td>
<td>30</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$M_{35,43}$ ***</td>
<td>23</td>
<td>$M_{36,42}$ **</td>
<td>19</td>
<td>$M_{60,61}$</td>
<td>5</td>
</tr>
<tr>
<td>$M_{59,62}$</td>
<td>20</td>
<td>$M_{44,50}$ **</td>
<td>16</td>
<td>$M_{38,40,46,48}$ **</td>
<td>20</td>
</tr>
<tr>
<td>$M_{56,65}$</td>
<td>16</td>
<td>$M_{47}$</td>
<td>25</td>
<td>$M_{55,58,63,66}$</td>
<td>12</td>
</tr>
<tr>
<td>$M_{52,53}$</td>
<td>4</td>
<td>$M_{45,49,51,54}$</td>
<td>20</td>
<td>$M_{57,64}$</td>
<td>8</td>
</tr>
</tbody>
</table>

*Not compound transistors.
**Body-contact transistors.
***Body-contact transistors and W=650 nm.
Figure 4.1: OTA frequency response.

Figure 4.2: Frequency response including PVT variations.

<table>
<thead>
<tr>
<th>Specification</th>
<th>Worse case</th>
<th>Typical case</th>
<th>Best case</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gain [dB]</td>
<td>58</td>
<td>60</td>
<td>64.5</td>
</tr>
<tr>
<td>GBW [MHz]</td>
<td>300</td>
<td>350</td>
<td>500</td>
</tr>
<tr>
<td>PM [°]</td>
<td>50</td>
<td>53</td>
<td>52.5</td>
</tr>
</tbody>
</table>

Table 4.2: Frequency response results.
4.2 Characterization

4.2.2 Input-output ranges

Due to the integration with the input stage, it is clear that the OTA will have full input swing. Figure 4.3 shows a PVT simulation with input common mode voltage variations and the bottom half of figure shows a square signal on each input, which has a common mode voltage variation over the complete available voltage. The top half of the figure shows the differential output, and demonstrates that the amplifier works regardless the input common mode voltage. However, in the extreme cases (low and high common mode level) some variations in the response were observed, due to the extreme cases have different gain values (as discussed in chapter 2), but the amplifier is still operating properly.

Although previous simulation show that the output signal also has full swing, it is only valid for digital signals or comparison functions, but for analog signals or its processing it is not a valid measurement. Figure 4.4 shows the DC input-output characteristics for single and differential outputs, which provides a measurement for the output range. The specification for the output range is 1.2 V, which is measured from this figure, but must be verified through distortion simulations in order to to obtain an accurate measurement. The obtained result is a reasonable value, taking into account that the output branches have six single transistors per column to form two compound transistors. These two transistors are very important because they provide high impedance nodes to accomplish the gain specification, and for these reason the number of transistors at the output cannot
be reduced and try to improve the output range. Figure 4.5 shows a PVT simulation, the results show considerable variations on single outputs, but is clear that the differential operation improves the behavior and always establishes the output common mode value at the desired value. It is due to the PVT variations producing equal changes on both sides of the circuit, which are eliminated by the subtraction at the output.
4.2 Characterization

4.2.3 Time response

Figure 4.6 shows three configurations to measure the slew rate parameter. The left scheme takes a differential measurement, but allows the signal flow through the feedback path modifying the measurement. The middle scheme only takes a single measurement and the real expected value is differential. On the other hand, the right scheme measure the true differential parameters, because the feedback is made with four resistor in a unity feedback configuration, and a proper resistors value prevents the signal flow through the feedback path. Figure 4.7 shows the circuit response to square signal input, due to circuit’s symmetry an expected equal positive and negative slew rate is expected. Table 4.3 shows the results.

Figure 4.8 shows the time response with PVT variations for square signal. It is very clear that all the samples are consistent in the time domain.
### 4.2.4 CMRR

Under typical conditions the measurement of differential Common Mode Rejection Ratio (CMRR) is wrong, because the ideal operation and signal subtraction produces an ideal measurement. One option is to measure the single output instead of the differential, and divide the differential gain by the measured value. But this type of measurement is only useful to obtain an approximate value, for this reason the best choice is to perform a monte-carlo analysis, in which the differential output is a realistic value, and the differential gain could be divided by the measurement obtaining a real value.

Figure 4.9 shows the measurement on a single output. The result for low frequency is very good, and the frequency range of interest remains a high value. Figure 4.10 shows the histogram for 200 simulations in the monte-carlo analysis, in which was observed a trend between 140 and 170 dB. The results of the monte-carlo analysis are so positive because more than 80% of the samples are upper 100 dB, and the average value is 150 dB.
The outstanding result for CMRR specification (including mismatch) is due to the wide use of the FDP cell, it is because using this structure is more difficult that the transistors get out from the desired operation point, and the correct biasing remain despite process variations. Also, the stability of the transconductance and the explained design considerations makes that the variations have not high impact on this specification. These reasons are also valid to explain the conclusive measurements over the next specification.
4.2.5 PSRR

The Power Supply Rejection Ratio (PSRR) measurement was also made through monte-carlo analysis in order to obtain realistic values for this specification. Figure 4.11 shows a couple of samples for positive and negative PSRR measurements to show the frequency response of this specification. Figures 4.12(a) and 4.12(b) shows the histogram for 200 simulations, in each case the result is extremely conclusive with respect to the value of the specification, for both cases it is 60 dB.
4.2 Characterization

4.2.6 Noise

Figure 4.13 shows the input referred noise in the two major units of measurement, the result is positive since the thermal noise is equivalent to 17 nV/√Hz, which is a low value taking into account the noise level of the low noise amplifiers. Also, this result is consistent with the noise levels shown in the technology documentation.

4.2.7 Distortion

A big concern for this type of technology is the distortion parameter, because the transistor parameters are being modifying along the time axis. This kind of distortion occurs due to the floating body and its effects, as explained in chapter 1. For this reason the design was modified and the size of transistors $M_{35,36,42}$ was changed. To this circuit is proposed a maximum distortion of 0.8% for the maximum output voltage (1.2 Vpp).

Figure 4.14 shows some measurements of distortion with respect to the signal’s maximum output voltage, this measure was made for a sinusoidal input signal with f=100 KHz. For all the output voltages of the defined output range, the distortion value is less than 0.8%. Figure 4.15 shows the distortion for signals with f=1 MHz, although the frequency is higher with respect to the previous measure, the result is better since the output voltage reached higher values with less distortion. For all cases, the spectrum shows that
the second harmonic component is eliminated by the differential operation (also all even components), and the major contribution to distortion is made by the third harmonic. Third harmonic elimination schemes can be used to reduce the same component (third harmonic) in order to create a high linear amplifier.

4.2.8 Offset

Finally, figure 4.16 shows the histogram of monte-carlo simulation for the offset measurement, it is clear that the mismatch between differential pairs generates an equivalent
signal which is amplified in the high impedance nodes, generating imbalance between the positive and negative outputs, therefore a considerable offset value of $940 \mu V$ referred at the input is obtained. This is one of the few disadvantages that involves the extensive use of differential pair structures since the mismatch between differential pair transistors generates high offset values, but in the literature there are several techniques to reduce the offset value.

Table 4.4 summarize the OTA specifications, the result demonstrate that it is possible to develop useful specifications for amplifiers in nanometer SOI technologies. In addition, it was verified that the designed input stage could be integrated in a simple way providing full input swing. This is the first work of its type reported with 1 V on supply voltage, because the previous works [3, 9] in the same technology used 1.3 V. The obtained differential gain doubles the value obtained in [3] including the attenuation produced by the input stage. Other outstanding specifications are related with the rejection ratios and noise, the obtained values were validated through monte-carlo simulations, and indicate that all the external factors which could harm the signal are very faint. The power consumption is relatively high because a robust circuit always involves additional branches in order to control or compensate the variations, this is the trade-off for robust circuits.

The next chapter will summarize the main conclusions and proposals obtained in this work and at the same time will propose suggestions in order to improve or expand this work.

![Offset measurement with monte-carlo analysis.](image)
### Specification Value

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Supply voltage</td>
<td>1 V</td>
</tr>
<tr>
<td>Differential gain</td>
<td>60 dB</td>
</tr>
<tr>
<td>GBW</td>
<td>350 MHz</td>
</tr>
<tr>
<td>Phase margin</td>
<td>53°</td>
</tr>
<tr>
<td>Load capacitance</td>
<td>200 fF</td>
</tr>
<tr>
<td>Differential output range</td>
<td>1.2 V</td>
</tr>
<tr>
<td>Slew rate</td>
<td>232 V/µs</td>
</tr>
<tr>
<td>Power consumption</td>
<td>2.6 mW</td>
</tr>
<tr>
<td>Settling time @ 0.1%</td>
<td>19 ns</td>
</tr>
<tr>
<td>CMRR</td>
<td>150 dB</td>
</tr>
<tr>
<td>PSRR+,−</td>
<td>60 dB</td>
</tr>
<tr>
<td>ICMR</td>
<td>Full swing</td>
</tr>
<tr>
<td>Input referred noise</td>
<td>17 nV/√Hz</td>
</tr>
<tr>
<td>THD @ $V_{out_{diff}}=1.2$, $f=1$ MHz</td>
<td>0.25%</td>
</tr>
<tr>
<td>Input referred $Offset$</td>
<td>1 mV</td>
</tr>
</tbody>
</table>

Table 4.4: Final OTA specifications
Chapter 5

Conclusions and Future Work

The previous chapters have provided important information about how analog design can remain in nanometer technologies. There are the two main concerns in nanometer technologies: the transistors in this type of technologies are not suitable to develop useful specifications in analog circuits like amplifiers; with smaller sizes on transistors, the uncertainty in fabrication processes, environmental conditions and second order effects, the variability in the circuit specifications raises significantly. Considering the above two concerns, the below summarizes the main contributions of this work and how it can be expanded upon and improved.

5.1 Conclusions

This work proposed and also exposed some circuits, criteria and considerations, in order to obtain robust and useful specifications for OTA’S. However, the propositions made can easily be expanded and applied to different circuits, to improve behavior, regardless of technology type and scale, as outlined below.

- A new topology for rail-to-rail input stage with constant transconductance was proposed. The transconductance and gain specifications are robust regardless of common mode input voltage or PVT variations. Moreover, this stage can operate properly over the complete input range (100% of available voltage) with a extremely minimum change in output common mode voltage. For these reason this stage can be implemented or integrated in almost all amplifiers.

- A new way to obtain constant and robust transconductance was proposed, it is the emulation of current switching through feedback differential pairs, feedback current mirrors, and sub-threshold operation to reduce the changes produced by process
and voltage variations. Also, the use of stages with opposite behavior with respect to temperature in order to compensate its effects.

- A cause was determined for low frequency gain variation in the flat-band of amplifiers made in SOI nanometer technology. In the same way, an effective solution through body-contact transistors in specific connections was proposed.

- The usefulness of matrix transistors in nanometer technologies was verified, in order to improve the behavior with respect to mismatch, PVT and SCE. Also, it was determined that matrix transistors contribute to reduce the low frequency gain variation, and are the only choice to obtain different transistor sizes in technologies with several restrictions in transistor sizing.

- A new high gain OTA scheme without cascode structures was proposed. This scheme obtained 67 dB with only two stages in 45 nanometer technology, this gain value is comparable with conventional two stages amplifiers in micrometer technologies. Despite high gain value, others specifications such as GBW or power consumption were not significantly affected.

- Additional considerations to achieve robust gain stages with respect to commonly techniques were proposed.

- Besides the widely known benefits of the FDP structure, it was verified that this structure improves the circuit performance with respect to PVT variations and allows the use of more complex current mirror structures without reducing dynamic range.

- Although the aim of this work focuses on PVT variations, the same techniques and schemes proved its efficiency including mismatch for some specifications.

- With the easy integration of the input and gain stages, the use of input stage to provide in a easy way full input swing, with any changes in transistors sizing was verified.

- The final specifications shows that robust amplifiers with good performance in all the specifications for nanometer SOI technologies could be developed.
5.2 Future Work

With the development of this work arises new interesting topics to complement and enhance the current work. On the other hand, some tasks, simulations and analysis must be done to finish the design flow for analog circuits in nanometer technologies. There are:

- It will be necessary to study and characterize the body section in body-contact transistors to analyze its feasibility in different applications such as CMFB, amplifiers, special filters (logarithmic) and multipliers among others. On the other hand conducting a deepest analysis over the charge variation along time in the body and its effects over different circuits is also suggested.

- Due to the technology restricted sizing the layout stage represents a big concern. This is due to the technology incorporating many more layers than conventional technologies and the use of matrix transistors, which raises the complexity in the layout stage. However, the restrictions over the sizing could allow the automation of the layout in a similar way to that of digital circuits.

- Establish some criteria in other types of circuits that allows the making of a robust design in a clearer way.

- During the design and simulation with the SC-CMFB circuit it was observed that the couple of noise in the signal due to the switching it is not negligible. In signal processing circuits that employs switched capacitor must be carefully designed in order to avoid noise and distortion. On the other hand, the low available voltage causes some switches not to work properly and in circuits of precision this issue cannot be neglected.

- The most common way to try to compensate analog circuits is through biasing, for this reason it is desirable to develop a variety of biasing circuits widely characterized in order to make easy and fast compensations in any design.

- Incorporate some techniques in order to reduce the circuit offset, and try to reduce the power consumption without losing robustness.
Bibliography


